# Physics 224 The Interstellar Medium

Lecture #8

- Part I: Few last points on the "curve of growth"
- Part II: Ionization Processes
- Part III: Recombination Processes



where line profile is:

$$\phi_{\nu} = \frac{1}{\sqrt{2\pi\sigma_{v}^{2}}} \int_{-\infty}^{\infty} e^{-v^{2}/2\sigma_{v}^{2}} \frac{4\gamma_{u\ell}}{16\pi^{2}(\nu - (1 - v/c)\nu_{u\ell})^{2} + \gamma_{u\ell}^{2}} dv_{\ell}$$

\*note no analytic formula for solution of integral









### as optical depth at line center becomes >1, $\, I_{ u,0}/I_0 ightarrow 0$



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eventually "damping wings" also get close to optical depth ~1



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# Absorption Lines

"Linear"  $W \propto N$   $\tau_o \ll 1$ 

"Flat" wave  $W \propto b \sqrt{\ln(N/b)}$   $10 \leq \tau_o \leq 10^3$  or "Logarithmic"

"Damped"  $W \propto \sqrt{N}$   $\tau_o \geq 10^4$ 

$$au_o = rac{\pi^{1/2}e^2}{mc}rac{\lambda}{b}Nf$$
 optical depth at line center



# Summary of Opt/UV Absorption Lines

- $E_{ul}$  is big, don't worry about stimulated emission, most in ground state.
- Line profile is Voigt (convolution of Gaussian with natural broadening)
- In low optical depth limit, only the Gaussian part matters, EW (equivalent width) is proportional to N (column density).
- Once line center saturates, EW has a "flat" dependence on N (i.e. sqrt(log(N))). Bad regime for measuring N!
- At very high optical depth, Lorentzian wings are important and EW depends on sqrt(N), can measure N from EW again.

## Ionization Processes

## **Ionization Processes**





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# **Ionization Processes**


## **Ionization Processes**



Cross section can be determined analytically for Hydrogen (and "hydrogenic" ions - those with 1 e- remaining)

when  $hv > 13.6 Z^2 eV$   $\sigma_{\rm pi}(\nu) = \sigma_0 \left(\frac{Z^2 I_{\rm H}}{h\nu}\right)^4 \frac{e^{4-(4 \tan^{-1} x)/x}}{1 - e^{-2\pi/x}}$ where:  $x = \sqrt{\frac{h\nu}{Z^2 I_{\rm H}}} - 1$ 

and "cross section at threshold" is

$$\sigma_0 = \frac{2^9 \pi}{3e^4} Z^{-2} \alpha \pi a_0^2 = 6.304 \times 10^{-18} Z^{-2} \text{ cm}^{-2}$$

~0



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Cross section complexity increases with multiple electrons.



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Cross section complexity increases with multiple electrons.



"absorption edge" due to K shell (the 1s shell)

at binding energy of K shell cross section increases sharply

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<u>Note:</u>

cross section of C and O and other metals far exceeds H at high energy

Even though they are less abundant, <u>metals dominate</u> <u>PI rate of gas at</u> <u>high energies.</u>



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rate per volume ~  $n_{atom} n_{collider} \sigma c$ 

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$$\zeta_{pi} = \int_{\nu_1}^{\infty} \sigma_{pi}(\nu) \ c \left(\frac{u_{\nu}}{h\nu}\right) d\nu$$
 minimum energy for ionization number density of photons

![](_page_48_Figure_0.jpeg)

http://hyperphysics.phy-astr.gsu.edu/hbase/atomic/auger.html

## **Ionization Processes**

![](_page_49_Figure_1.jpeg)

## **Ionization Processes**

![](_page_50_Figure_1.jpeg)

# Secondary Ionizations

 $E_{pe} = h\nu - I_s$ 

Energy of ejected photoelectron

difference between photon energy and ionization potential

For x-ray ionization E<sub>pe</sub> can be big! May go on to ionize other atoms/ions in the gas.

Secondary ionization rate depends on  $E_{\rm pe}$  and ionization state of the gas.

## Part II: Ionization Processes

![](_page_52_Figure_1.jpeg)

![](_page_53_Figure_0.jpeg)

![](_page_53_Figure_1.jpeg)

$$k_{ci} = \int_{I}^{\infty} \sigma_{ci}(E) \ v \ f(E) dE$$

integral of cross section over Maxwellian velocity distribution

# **Collisional Ionization**

![](_page_54_Figure_1.jpeg)

At higher E, cross section ~ 1/E (can show this from the impact approx from Lecture 2)

## Part II: Ionization Processes

![](_page_55_Figure_1.jpeg)

# Cosmic Ray Ionization

![](_page_56_Figure_1.jpeg)

Cosmic ray energy flux is dominated by protons.

$$\xi_{\rm CR} = 4\pi \int_{E_{\rm min}}^{\infty} \sigma_{\rm ci}(E) E \frac{dF}{dE} \cdot \frac{dE}{E}$$

Similar to before but velocity distribution is <u>not Maxwellian</u>

Big uncertainties in CR flux at low energies due to solar wind.

# Cosmic Ray Ionization

![](_page_57_Figure_1.jpeg)

CR ionization is very important in dense gas, where extinction by dust and other absorption has blocked most photons.

Will come back to this in discussing molecular clouds!

# Part III: Recombination Processes

#### Part III: Recombination Processes

![](_page_59_Figure_1.jpeg)

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![](_page_60_Figure_1.jpeg)

![](_page_61_Figure_0.jpeg)

 $E_{photon} = I_{nl} + E_{kinetic}$ 

 $I_{nl}$  = ionization potential from nl

Given photoionization cross section from before, we can use detailed balance to work out radiative recombination cross section.

Milne Relation:

$$\sigma_{\rm rr}(E) = \frac{g_{\ell}}{g_u} \frac{(I_{X,u\ell} + E)^2}{Em_e c^2} \sigma_{\rm pi}(h\nu = I_{X,u\ell} + E).$$

$$X^+_{\mathcal{U}} + e^- \to X_{\mathcal{C}} + h\nu_{\mathcal{C}}$$

![](_page_63_Figure_1.jpeg)

Energy not to scale

# Radiative Recombination $M = I_{nl} + E_{kinetic}$

![](_page_64_Figure_1.jpeg)

Hydrogen

Energy not to scale

1s ——

![](_page_65_Figure_1.jpeg)

Energy not to scale

![](_page_66_Figure_0.jpeg)

#### Photon can ionize another H atom immediately if there is enough H around!

"Case A": optically thin to ionizing radiation, every ionizing photon from a recombination can escape good approx for hot, collisionally ionized gas

"Case B": Optically thick to ionizing radiation, recombinations to n=1 do not reduce ionization state of gas

good approx for "HII regions" = photoionized nebulae around young, massive stars

"Case A": optically thin to ionizing radiation, every ionizing photon from a recombination can escape

$$\alpha_A(T) = \sum_{n=1}^{\infty} \sum_{\ell=0}^{n-1} \alpha_{n\ell}(T)$$

total recombination rate = sum of recombination rates to all levels

"Case B": Optically thick to ionizing radiation, recombinations to n=1 do not reduce ionization state of gas

$$\alpha_B(T) = \sum_{n=2}^{\infty} \sum_{\ell=0}^{n-1} \alpha_{n\ell}(T) = \alpha_A(T) - \alpha_{1s}(T) \qquad \text{same but 1s rate is omitted}$$

![](_page_69_Figure_1.jpeg)

For all but the highest n levels, collisions are much slower than radiative transitions -> recombination produces a characteristic spectrum of Hydrogen emission lines.

![](_page_70_Figure_1.jpeg)

allowed radiative decays for: n > n' and  $l - l' = \pm 1$ 

Einstein A coefficients + selection rules -> "branching ratios"

![](_page_71_Figure_1.jpeg)

For Case A this is straightforward.
## **Radiative Recombination**



For Case B, need to recognize that cross section for Lyman transitions is big, bigger than even photoionization cross section.

$$ext{for example:} ag{T_{Ly\alpha}} = 8.0 imes 10^4 \left(rac{15 ext{ km s}^{-1}}{b}
ight) au_{ ext{LyC}}$$

## **Radiative Recombination**



Lyman photons will be absorbed immediately. "resonantly scattered" with small changes in freq until a non-Lyman transition occurs

## **Radiative Recombination**



Case B: rates for Lyman transitions -> 0 distributed instead among other transitions

## **Other Recombination Processes**

- Dielectronic: capture of incoming electron excites one of the other bound electrons -> 2 excited e-
- Dissociative: molecular ion captures e-, dissociates
- Charge exchange: one important reaction is  $O^+ + H < -> O + H^+$
- Neutralization by dust grains

Credit: NASA,ESA, M. Robberto (Space Telescope Science Institute/ESA) and the Hubble Space Telescope Orion Treasury Project Team